

Strategies to reduce the dynamic disorder in molecular semiconductors

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The dynamic disorder is known to be one of the crucial parameters limiting the charge carrier transport in molecular semiconductors and a parameter that cannot be easily controlled through known design rules. To identify much needed guiding principles we evaluate the dependence of dynamic disorder on a large number of molecular and crystal characteristics for a set of almost five thousand known molecular semiconductors. We find that the strength of dynamic disorder is highly correlated with the gradient of transfer integral, a property easily computable for any molecular orientation. We also show that orientations of molecular pairs with just few atoms in contact are more likely to yield low dynamic disorder. This observation is highly counterintuitive as for years the focus has been to maximize the number of π -stacked atoms. Other properties with meaningful influence on the dynamic disorder include the presence of alkyl chains, the strength of transfer integral and the presence of heavy atoms. The findings of this work provide important design principles for low-disorder high-mobility molecular semiconductors.

Small organic molecules present a potential application for flexible, low-cost, and light-weight electronic devices.^{1–4} The performance of these devices strongly depends on the efficiency of charge transport processes and, accordingly, discovering and designing materials with high carrier mobilities is one of the major research objectives in the field of organic electronics.^{5–10} Molecular semiconductors are held together by weak van der Waals (vdW) forces, thereby, the thermal motion of molecules even at room temperature, known as the *dynamic disorder*, is large enough to cause transfer integrals fluctuations,¹¹ with a magnitude comparable to that of the average transfer integral.¹² There is a growing body of evidence that the charge mobility and, subsequently, the performance of electronic devices is largely affected by the strength of dynamic disorder.^{13–16} This effect, which is a manifestation of nonlocal electron-phonon couplings, is independent of the specific model of transport.^{17–23} While there are other important parameters, e.g. the molecular area,²⁴ the local electron-phonon coupling,^{25–27} the two-dimensional nature of transport,^{20,28} the dynamic disorder remains the one without clear design rules that can help the discovery of new high-performance materials. As shown in Ref.²⁴, these important parameters are either uncorrelated or “constructively” correlated. Specifically, reducing the dynamic

disorder would not present any detrimental impacts on the other crucial parameters affecting the charge carrier mobility. At present, except the simple principle of employing stiff structures,²⁹ no generic practical strategies are known for designing structures with a small dynamic disorder. Understanding what can cause a low degree of dynamic disorder is, therefore, one of the key points which can open up vast opportunities for designing high mobility materials.

The evaluation of dynamic disorder, on the one hand, is a computationally extremely expensive task requiring the transfer integrals' gradients and the crystal phonons calculations.^{30,31} On the other hand, the low-energy nature of thermal fluctuations prevents them to be feasibly accessible experimentally.^{16,32–34} All together has led to the situation where the existing works report calculations of this parameter on one³⁵ or few³⁶ molecules with the requirement of millions of CPU hours for the state of the art calculations.³⁷ A novel multi-scale Quantum Mechanics/Molecular Mechanics (QM/MM) methodology developed in ref.²⁴ enabled us to significantly speed up the dynamic disorder calculations and create the first large database of computed dynamic disorders (~5,000 entries – a subset of Cambridge Structural Database (CSD)³⁸). The aim of the present work is to utilize this unique large set of data to evaluate what are the major characteristics of the structures representing a low degree of dynamic disorder. We identify a list of characteristics that could potentially be linked with the degree of dynamic disorder and we establish if the correlation is meaningful.

Dataset. In the considered database, the materials possess two important characteristics: their largest transfer integral $|J|$ between HOMO orbitals localized on different molecules is greater than 0.1 eV and their valence bands expand in two dimensions (a desirable property for the charge transport in molecular semiconductors^{20,28}). From each entry, we consider the molecular pair with the largest J , the corresponding dynamic disorder σ (i.e. the standard deviation of J fluctuations at room temperature³⁰) and the gradient of the transfer integral ∇J with respect to the displacement of the atomic coordinates. The latter quantity can be visualized as vectors applied on each atom and the displacement along such vectors would cause the largest variation of transfer integral as illustrated in Figure 1. J and ∇J are electronic properties only depending on the mutual orientation of the molecules, while σ also depends on the phonons (shown schematically in Figure 1) and temperature – set to 290 K in this work. For convenience, the “relative dynamic disorder” defined as $\Delta = \sigma/J$ is also considered. The distributions of the data constituting the foundation of the present study (i.e. $|J|$, ∇J , σ and Δ) are shown in the lower rows of Figure 1. As can be seen, (i) the variation of the dynamic disorder σ is of the same order of magnitude as the transfer integral itself - a fact that has been noted in the past³⁹ and essentially the reason for its importance; (ii) the distribution of the dynamic disorder is quite similar to that of the transfer

integrals' gradients (this aspect will be outlined in further detail later); (iii) The distribution of Δ is broad, peaked around 0.5 in agreement with many works in literature,²⁰ with a useful fraction of materials with small Δ that can be used to identify patterns in materials with a low degree of dynamic disorder. The materials are classified in three groups such that the first group represents the small relative dynamic disorder of $\Delta \leq 0.3$ (group A), the second one an intermediate regime of $0.3 < \Delta \leq 0.7$ (group B) and the last one incorporates the highly fluctuating structure $\Delta > 0.7$ (group C). This classification, highlighted in the last panel of Figure 1, allows one to better understand the impact of structural characteristics on the degree of dynamic disorder.

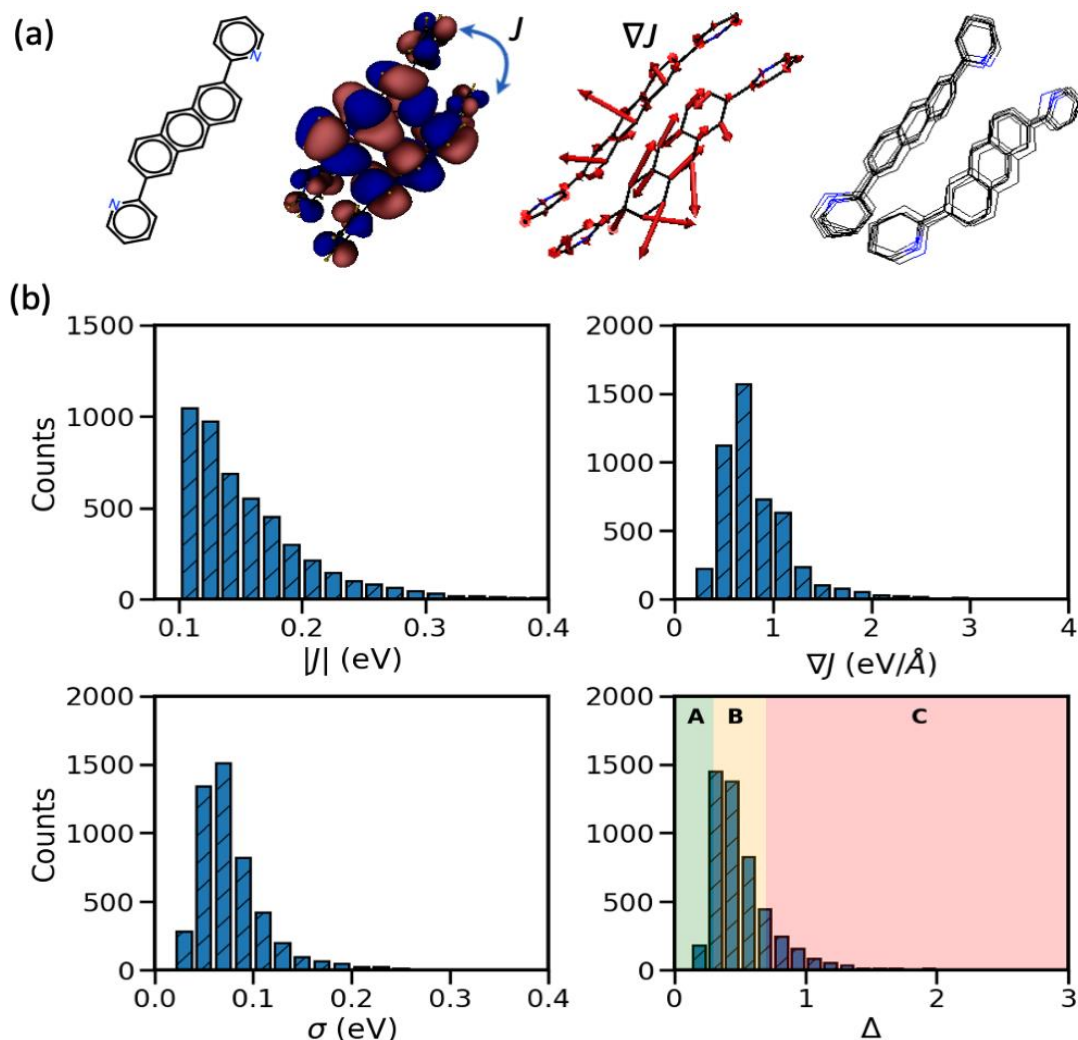


Figure 1. (a) From left to the right: chemical structure of material identified as OKIKUQ in CSD; the transfer integral J which is proportional to the overlap of HOMO orbitals of the neighboring molecules as represented; the gradient of the transfer integral ∇J – the red arrows illustrate the direction and relative magnitude of the nuclear deformation; the phonons – the overlapped geometries of 10 vibrating OKIKUQ molecules at 290 K are shown. (b) Distribution of the largest transfer integral, the associated gradient of the transfer integral, dynamic disorder, and the relative dynamic disorder for the considered $\sim 5k$ molecular semiconductors.

Considered parameters. In order to identify possible correlations between the strength of dynamic disorder and the molecular/crystal characteristics, we have identified a list of characteristics that could potentially be linked with the degree of dynamic disorder. A large number of properties that we have considered and related to the molecular topology, the stoichiometry, the frontier orbital energy levels, descriptors of the HOMO orbitals and crystal descriptors did not display any appreciable correlation with the strength of dynamic disorder and the corresponding correlation factors with the original motivation for considering them is reported in the Supplementary Information (SI). In the main manuscript, we discuss properties with appreciable correlation with the dynamic disorder that can be used for the design of new materials. The key data and their correlations are summarized in a correlation matrix in Figure 2. Their variation range is represented in a series of box plots in the right side of the figure. The box plots help to understand how the variation range of a parameter changes within different groups. As such, as can be seen, for parameters negatively correlated to the dynamic disorder, the trend of parameter variation in going from group A to group C is descending while an opposite scenario applies to the positively correlated parameters. In the following, we discuss each key property and its correlation with the others.

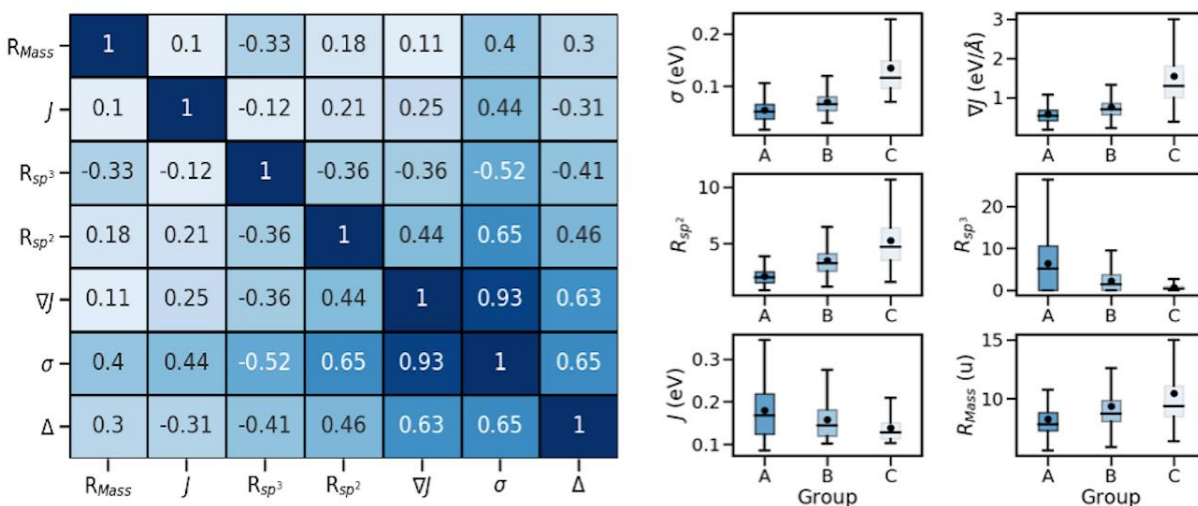


Figure 2. (Left) The Spearman's rank correlation between parameters. (Right) The variation range of parameters correlated with the relative dynamic disorder (i.e. σ , ∇J , R_{sp^2} , R_{sp^3} , J and R_{Mass}) among defined categories of A, B, and C depicted on a series of "box plots". The box limits represent the first (Q_1) and third quartiles (Q_3), with a line and a small circle representing the median and the mean value, respectively.

(i) Strength of the transfer integral's gradient (∇J). As shown in Figure 2, there is a significant positive correlation between the dynamic disorder σ and the gradient of the associated transfer integral ∇J , suggesting that the gradient of the transfer integral is the main parameter determining the strength of

dynamic disorder. This behaviour which is visualized in Figure 3 was partially anticipated by the work of Landi et al.³¹ and implies that the dynamic disorder is mostly but not entirely an electronic property. In a similar analysis, Schweicher et al.⁴⁰ have evaluated the transfer integrals as a function of relative intermolecular shift along the molecular long axis z . Their results indicate that if the equilibrium position in a molecule is in the immediate proximity of a “sweet spot”, where the transfer integral (plotted as a function of z) shows an extremum, small values of the derivative and dynamic disorder are expected. Accordingly, given the relative position of two molecules, one can predict if the dynamic disorder is going to be large regardless of the surrounding. This observation is of particular importance as (i) it can justify the use of approximate phonons^{24,31,41} for evaluating the dynamic disorder, and (ii) allows one to search for materials with small transfer integrals’ gradients rather than small dynamic disorder.

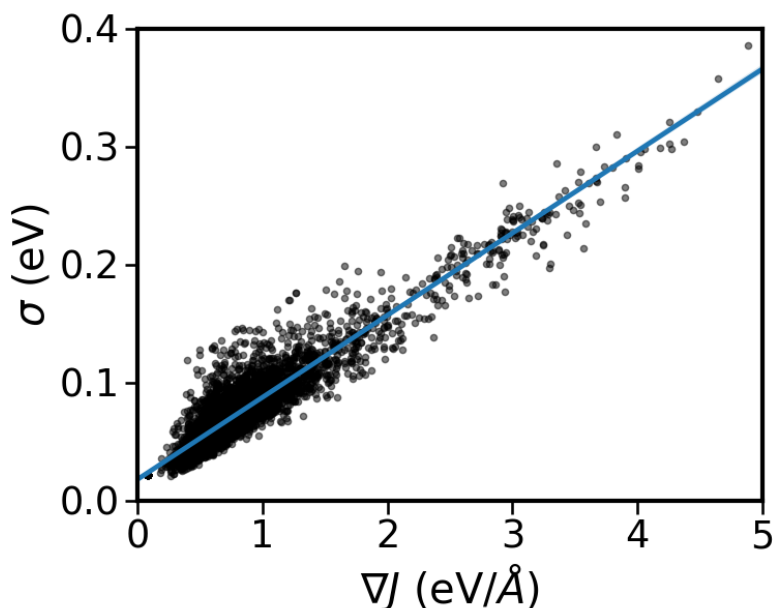


Figure 3. The correlation between σ and ∇J for the considered database composed of $\sim 5k$ molecular semiconductors.

(ii) The pairing geometry of the molecules (R_{sp^2}). The pairing geometry of molecules quantified by the number of sp^2 -hybridized atoms in vdW contact (normalized to the total number of atom and expressed in percentage) is another important parameter that affects the strength of dynamic disorder substantially. In the analysis, only atoms contributing to the HOMO orbital are considered. Furthermore, the atoms are assumed in contact if the distance between them is shorter than the sum of their vdW radii (values extracted from ref.⁴²) multiplied by a constant value. The correlation matrix of Figure 2 depicts a strong positive correlation (+0.65) between R_{sp^2} and the dynamic disorder σ (visualized in Figure 4). This high level of dependence of the dynamic disorder on the pairing geometry of molecules can be related to the

interaction between orbitals with many nodes. As such, in structures revealing smaller degrees of dynamic disorder, the molecular orbitals overlap takes place through the region of the orbital where there are not many nodes. This aspect was noted in refs.^{39,43}.

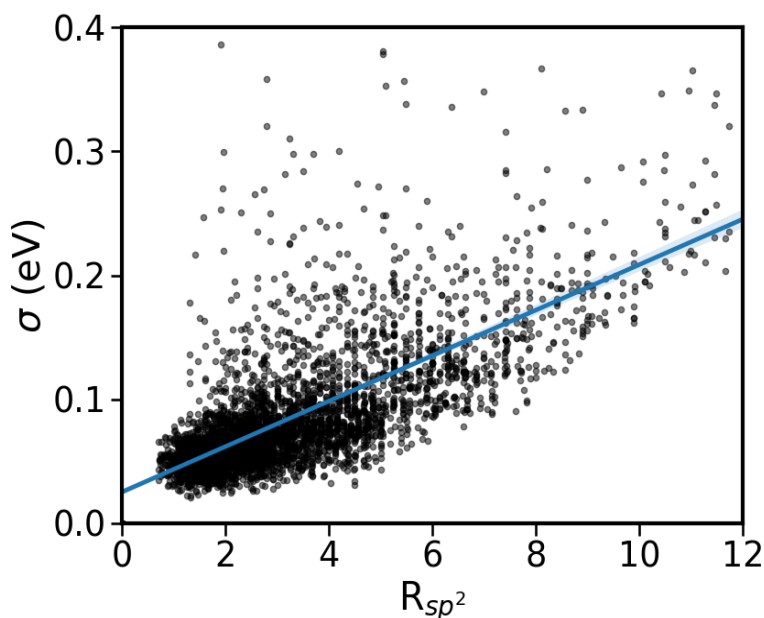


Figure 4. The correlation between σ and R_{sp^2} for the considered database of molecular semiconductors.

The concept of pairing geometry can be better understood from Figure 5 where representative examples of different values of R_{sp^2} are shown. As can be seen, the overlap between the two molecules increases for growing values of R_{sp^2} . The materials with smaller values of R_{sp^2} are arranged in a “head-to-tail” fashion, but with the conjugated cores of the interacting molecules not lying on the same plane. The head-to-tail arrangement of the molecules is highly counterintuitive. The field has tried for years to have the maximum π -stacking and our results are proposing that a minimum π -stacking represents another optimum (i.e. a lower degree of dynamic disorder). It has also to be noted that the correlation between R_{sp^2} and the relative dynamic disorder Δ is slightly weaker than that of σ . Nevertheless, due to the possibility of independent engineering of J , it does not diminish the importance of this parameter. This analysis suggests that molecular crystals with molecules interacting through the terminal ends of their conjugated core are potentially promising for smaller fluctuations.

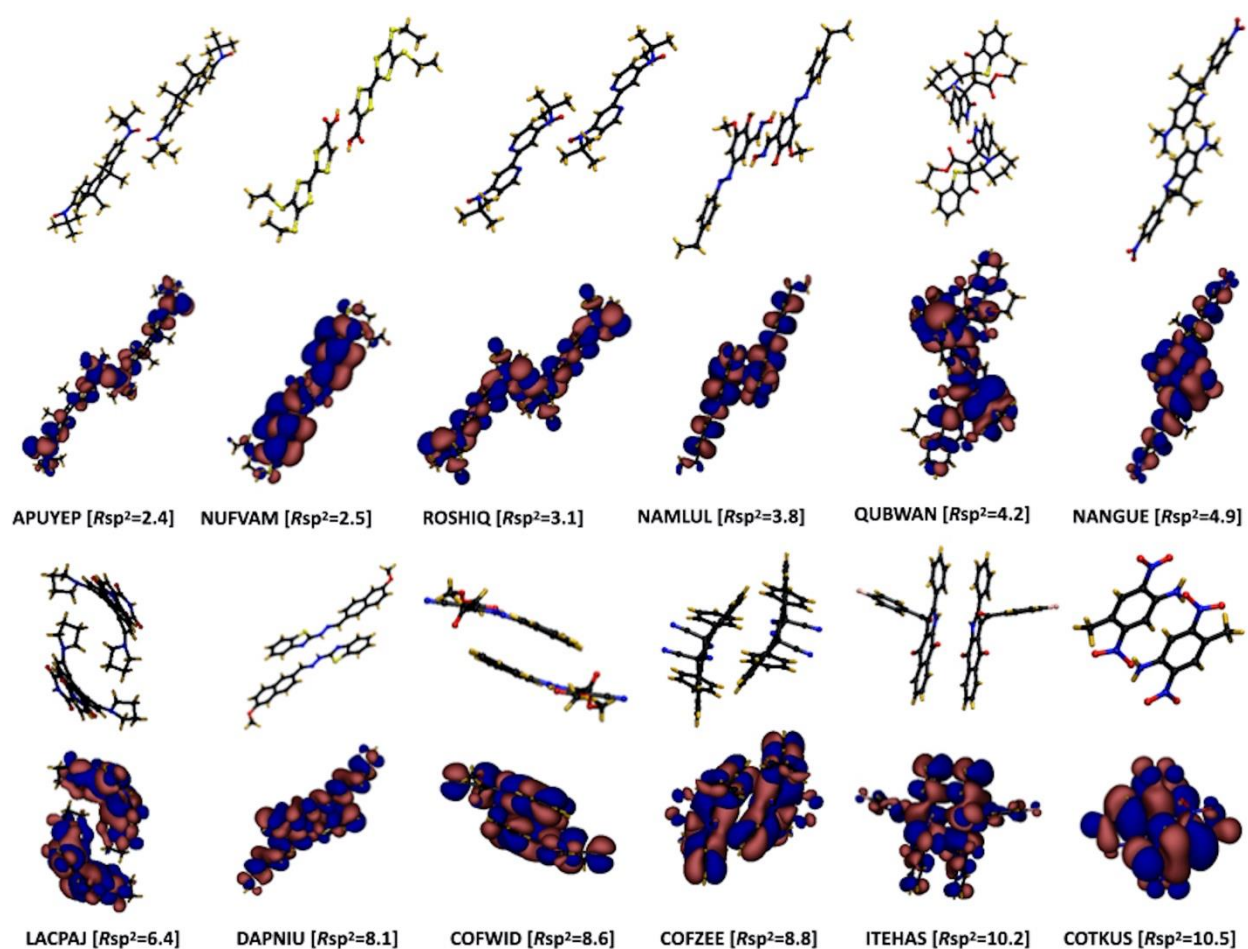


Figure 5. The pairing geometry of a selection of molecules with: (top two rows) small values of R_{sp^2} and (bottom two rows) higher values of R_{sp^2} . For each dimer structure, its DFT computed HOMO orbital is shown in the following row. The structures are labelled by their CSD identifiers and their corresponding value of R_{sp^2} is indicated (in percentage).

(iii) The presence of alkyl chains. The negative correlation between σ and the number of sp^3 -hybridized carbon atoms divided by the total number of atoms, denoted as R_{sp^3} , is significant (-0.52) meaning that the presence of alkyl chains (i.e. C_nH_{2n+1} group) can potentially suppress the thermal fluctuations. Similar to the case of R_{sp^2} , the correlation becomes slightly weaker when considering the relative dynamic disorder, however, the same scenario is present here and one can try to engineer J independently. According to the correlation matrix of Figure 2, R_{sp^3} correlates appreciably more with σ than ∇J suggesting that the attachment of the side chains can shift the vibration range of the conjugated core toward higher frequencies. A detailed analysis of this effect was recently reported by Schweicher et al.⁴⁰ who stressed the importance of alkyl side chains on shifting in-plane modes to higher frequencies which leads the energy fluctuations to be dominated by a single sliding mode. It is known that the phonons contribute to the dynamic disorder if they are thermally populated. This alteration in the vibrational frequencies leads

to a reduced number of low-frequency (i.e. thermally populated) modes that contribute to the dynamic disorder. Thereby, the side chains lead to a conjugated core more rigidly held in its equilibrium position and potentially are desirable to diminishing the dynamic disorder.^{37,44–46} In this context, an emerging design is two-dimensional molecular semiconductors with long side chains which have been agreed to reduce large amplitude motions.⁴⁷ It has also to be noted that the transfer integrals for the considered structures are sufficiently large implying that a balanced compromise of large transfer integral and small dynamic disorder can be achieved by proper design of molecules with alkyl side chains. In the best materials (i.e. those in group A) this might be achieved when the interacting molecules face the conjugated core of each other (Figure 6 – top row) or when the alkyl chain of one molecule interacts with the conjugated core of the other molecule (Figure 6 – bottom row). These conformations while providing a sufficiently large transfer integral avoid large amplitude thermal fluctuations.

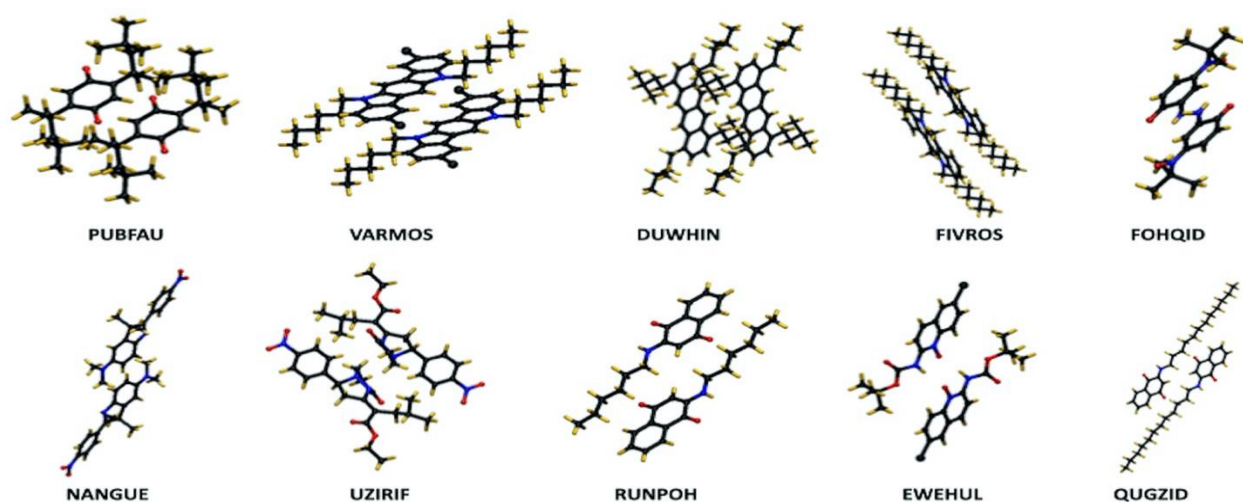


Figure 6. Examples of alkylated structures of group A. (Top panels) The interacting molecules face the conjugated core of each other, and (Bottom panels) the interaction happens partially through the alkyl chain of one molecule and the conjugated core of the other. Materials are labelled by their CSD identifiers.

(iv) Strength of the transfer integral (J). The correlation map reveals that the larger transfer integral J is moderately correlated with the larger dynamic disorder σ , as expected. Moreover, the relative dynamic disorder Δ is positively (negatively) correlated with σ (J) as anticipated from its definition. The ultimate role of increasing J is, therefore, to reduce the relative dynamic disorder. While it has been noted that increasing the transfer integral J has no significant impact on the charge carrier mobility if the relative disorder Δ is constant, according to the correlation matrix, increasing values of J contributes to a smaller relative disorder and consequently can boost the mobility.

(v) The ratio between molecular mass and number of atoms (R_{Mass}). Another important observation of the present work is the presence of a positive correlation between the strength of dynamic disorder and the presence of heavy atoms. To better quantify the trend, we have defined a parameter R_{Mass} which is a ratio between molecular mass and number of atoms. The positive correlation between R_{Mass} and the dynamic disorder suggests that the small molecules (i.e. those with fewer atoms) containing elements of heavier weight are expected to lead to higher degrees of dynamic disorder. Furthermore, it is notable that the correlation between R_{Mass} and ∇J is significantly smaller than that of σ implying that the effect of heavy atoms is predominantly vibrational. In fact, the involvement of the heavy atoms in the molecular structure leads to an increased number of low-frequency modes that contribute to the dynamic disorder and consequently leads to an increment in the strength of the dynamic disorder. Some early works have also shown a growing behavior of electron-phonon coupling with the involvement of heavy atoms.⁴⁸ In addition, the observed impact of heavy atoms is well in line with the results of experimental studies which predicts reduced mobility for the heavier isotope of a given structure.⁴⁹

Due to the computationally/experimentally demanding nature of dynamic disorder evaluations, the investigation of this property has been traditionally limited to a few structures with no possibilities to derive useful design rules. The screening of a large materials space is useful to confirm in a statistically more rigorous way the correlations that have been noted on small samples in literature and this work gives further support to ideas already presented and related to the beneficial effect of alkyl side chains or heavy atoms. However, the most useful findings are those allowing novel approaches to materials discovery. The results of this work point to two novel discovery strategies related to each other but different in the way they are implemented. The first insight is to use the gradient of the transfer integral ∇J as a simpler guide to the best possible arrangement of molecules in a molecular crystal to minimize the dynamic disorder. Its evaluation still requires the input from computational chemistry but without the computationally demanding evaluation of the crystal phonons. It can be useful to identify *in silico* convenient intermolecular arrangements combining low potential energy and low ∇J and to screen the output of predicted crystal structures.⁵⁰ The second strategy is possibly more appealing to bottom-up design and chemical intuition⁵¹ and it is based on the crystal engineering of molecules with strong head-to-tail interactions. These not only minimize ∇J , σ and Δ , but, if the molecule possesses a long axis, also increase the charge carrier mobility, which is proportional to the square of the intermolecular axis.²⁴ Furthermore, this is a strategy almost opposite to what is normally pursued in organic electronics, where the number of sp^2 hybridized atoms in contact tend to be maximized. A series of examples of such

arrangements identified from the CSD can serve as blueprints for the design of new molecules packing in similar fashion. It has to be noted that the implementation of these design principles in new materials with unknown crystal structures, would still require a set of trial-and-error evaluations. These practical guidelines, however, are expected to significantly reduce the search space and accordingly increase the success rate of trial and error methods. We believe these insights can provide practical strategies for reducing the degree of dynamic disorder and consequently increasing the mobility in molecular semiconductors.

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